

CALCULISTA

DISTRIBUIÇÃO POR FREQUENCIA GLOBAL E PARTE



Calculista (Todos candidatos)
- Total -

X	T	F	d	Fd	Fd ²	Fa
0 - 4		1	- 4	- 4	16	1
5 - 9		8	- 3	- 24	72	9
10 - 14		10	- 2	- 20	40	19
15 - 19		27	- 1	- 27	27	46
20 - 24		27	-	- 75		73 ← P
25 - 29		27	+ 1	+ 27	27	100
30 - 34		21	+ 2	+ 42	84	121
35 - 39		8	+ 3	+ 24	72	129
40 - 44		2	+ 4	+ 8	32	131
45 - 47						
		131		+ 101	370	
				+ 26		

$$M = 22,5 + \frac{26}{131} \times 5 \quad M_i = 20 + \frac{19,5 \times 5}{27}$$

$$M = 22,5 + 0,198 \times 5 \quad M_i = 20 + \frac{97,5}{27}$$

$$M = 22,5 + 0,990$$

$$M = 23,490$$

$$M_i = 20 + 3,611$$

$$M_i = 23,611$$

$$\sigma = \pm 5 \sqrt{\frac{370}{131} - 0,198^2}$$

$$M_o = (3 \times 23,611) - (2 \times 23,490)$$

$$\sigma = \pm 5 \sqrt{2,824427 - 0,039204} \quad M_o = 70,833 - 46,980$$

$$M_o = 23,853$$

$$\sigma = \pm 5 \sqrt{2,785223}$$

$$S = \frac{23,490 - 23,853}{8,340}$$

$$\sigma = \pm 5 \times 1,668$$

$$S = \frac{-0,363}{8,340}$$

$$\sigma = \pm 8,340$$

$$S = -0,044$$



$$Q_1 = 15 + \frac{13,75 \times 5}{27}$$

$$Q_3 = 25 + \frac{25,25 \times 5}{27}$$

$$Q_1 = 15 + \frac{68,75}{27}$$

$$Q_3 = 25 + \frac{126,25}{27}$$

$$Q_1 = 15 + 2,546$$

$$Q_3 = 25 + 4,676$$

$$Q_1 = \underline{17,546}$$

$$Q_3 = \underline{29,676}$$

$$Q = \frac{29,676 - 17,546}{2}$$

$$P_{15,87} = 15 + \frac{1,7897 \times 5}{27}$$

$$Q = \frac{12,130}{2}$$

$$P_{15,87} = 15 + \frac{8,9485}{27}$$

$$Q = \underline{6,065}$$

$$P_{15,87} = 15 + 0,331$$

$$P_{15,87} = \underline{15,331}$$

$$P_{84,13} = 30 + \frac{10,2103 \times 5}{21}$$

$$\overline{O.D.P.} = \frac{8,340}{\sqrt{262}}$$

$$P_{84,13} = 30 + \frac{51,0515}{21}$$

$$\overline{O.D.P.} = \frac{8,340}{16,186}$$

$$P_{84,13} = 30 + 2,431$$

$$P_{84,13} = \underline{32,431}$$

$$\overline{O.D.P.} = \underline{0,515}$$

$$\overline{O.M.} = \frac{8,340}{\sqrt{131}}$$

$$C.V. = \frac{100 \times 8,340}{23,490}$$

$$\overline{O.M.} = \frac{8,340}{11,445}$$

$$C.V. = \frac{834}{23,490}$$

$$\overline{O.M.} = \underline{0,729}$$

$$C.V. = \underline{35,504}$$

$$M - \sigma = 23,490 - 8,340$$

$$M - \sigma = \underline{15,150}$$



Calculista (Todos candidatos)

1ª parte

x	T	F	d	Fd	Fd ²	Fa
0-1	10	20	-2	-40	80	20
2-3	10	14	-1	-14	14	34
4-5	10	55	-	-54		89
6-7	10	42	+1	+42	42	131
		131		-12	136	

$$M = 5 - \frac{12}{131} \times 2$$

$$M_i = 4 + \frac{31,5}{55} \times 2$$

$$M = 5 - 0,092 \times 2$$

$$M_i = 4 + \frac{63}{55}$$

$$M = 5 - 0,184$$

$$M = 4,816$$

$$M_i = 4 + 1,145$$

$$M_i = 5,145$$

$$\sigma = +2 \sqrt{\frac{136}{131} - 0,092^2}$$

$$M_0 = (5,145 \times 3) - (4,816 \times 2)$$

$$\sigma = +2 \sqrt{1,038168 - 0,008464}$$

$$M_0 = 15,435 - 9,632$$

$$\sigma = +2 \sqrt{1,029704}$$

$$M_0 = 5,803$$

$$\sigma = \pm 2 \times 1,014$$

$$\sigma = \pm 2,028$$

$$P_{15,87} = 2 + \frac{0,7897}{14} \times 2$$

$$P_{84,13} = 6 + \frac{21,2103}{42} \times 2$$

$$P_{15,87} = 2 + \frac{1,5794}{14}$$

$$P_{84,13} = 6 + \frac{42,4206}{42}$$

$$P_{15,87} = 2 + 0,113$$

$$P_{84,13} = 6 + 1,010$$

$$P_{15,87} = 2,113$$

$$P_{84,13} = 7,010$$



$$\sigma_{D.P.} = \frac{2,028}{\sqrt{131 \times 2}}$$

$$\sigma_M = \frac{2,028}{\sqrt{131}}$$

$$\sigma_{D.P.} = \frac{2,028}{\sqrt{262}}$$

$$\sigma_M = \frac{2,028}{11,445}$$

$$\sigma_{D.P.} = \frac{2,028}{16,186}$$

$$\sigma_M = 0,178$$

$$\sigma_{D.P.} = 0,125$$

$$S = 4,816 - 5,803$$

$$\frac{2,028}{}$$

$$C.V. = \frac{100 \times 2,028}{4,816}$$

$$\frac{202,8}{4,816}$$

$$S = -0,987$$

$$\frac{2,028}{}$$

$$C.V. = \frac{202,8}{4,816}$$

$$\frac{42,110}{}$$

$$S = 0,487$$

$$C.V. = 42,110$$

$$Q_1 = 2 + \frac{12,75 \times 2}{14}$$

$$\frac{25,50}{14}$$

$$Q_3 = 6 + \frac{9,25 \times 2}{42}$$

$$\frac{18,50}{42}$$

$$Q_1 = 2 + \frac{25,50}{14}$$

$$\frac{18,21}{}$$

$$Q_3 = 6 + \frac{18,50}{42}$$

$$\frac{0,440}{}$$

$$Q_1 = 2 + 1,821$$

$$Q_3 = 6 + 0,440$$

$$Q_1 = 3,821$$

$$Q_3 = 6,440$$

$$Q = \frac{6,440 - 3,821}{2}$$

$$\frac{2,619}{2}$$

$$Q = 1,310$$

$$\frac{1,310}{}$$

$$Q = 1,310$$



Calculista - (Todos candidatos)

2ª parte

X	T	F	d	Fd	Fd ²	Fa
0 - 1		10	-2	-32	64	16
2 - 3		43	-1	-43	43	59
4 - 5		29	-	-75		88
6 - 7		26	+1	+26	26	114
8 - 9		12	+2	+24	48	126
10		5	+3	+15	45	131
		131		+65	226	
				-10		

$$M = 5 - \frac{10 \times 2}{131} \quad M_i = 4 + \frac{6.5 \times 2}{29} \quad M_o = (3 \times 4,448) - (2 \times 4,848)$$

$$M_o = 13,384 - 9,696$$

$$M = 5 - 0,076 \times 2 \quad M_i = 4 + \frac{13}{29} \quad M_o = 3,688$$

$$M = 5 - 0,152 \quad M_i = 4 + 0,448$$

$$M = 4,848 \quad M_i = 4,448 \quad C.V. = \frac{100 \times 2,622}{4,848}$$

$$\sigma = \pm 2 \sqrt{\frac{226}{131} - 0,076^2} \quad S = \frac{4,848 - 3,688}{2,622} \quad C.V. = \frac{262,2}{4,848}$$

$$\sigma = \pm 2 \sqrt{1,725191 - 0,005776} \quad S = \frac{1,160}{2,622} \quad C.V. = 54,084$$

$$\sigma = \pm 2 \sqrt{1,719415} \quad S = 0,448 \quad \sigma_M = \frac{2,622}{\sqrt{131}}$$

$$\sigma = \pm 2 \times 1,311 \quad P_{84,13} = 6 + \frac{22,2103 \times 2}{26} \quad \sigma_M = \frac{2,622}{11,445}$$

$$\sigma = \pm 2,622 \quad P_{84,13} = 6 + \frac{44,4206}{26} \quad \sigma_M = 0,229$$

$$P_{15,87} = 2 + \frac{4,7897 \times 2}{43} \quad P_{84,13} = 6 + 1,708 \quad \sigma_{D.P} = \frac{2,622}{\sqrt{262}}$$

$$P_{15,87} = 2 + \frac{9,5794}{43} \quad P_{84,13} = 7,708 \quad \sigma_{D.P} = \frac{2,622}{16,186}$$

$$P_{15,87} = 2 + 0,223 \quad \sigma_{D.P} = 0,162$$



$$Q_1 = 2 + \frac{16,75 \times 2}{43}$$

$$Q_1 = 2 + \frac{33,50}{43}$$

$$Q_1 = 2 + 0,779$$

$$Q_1 = \underline{2,779}$$

$$Q_3 = 6 + \frac{10,25 \times 2}{16}$$

$$Q_3 = 6 + \frac{20,50}{16}$$

$$Q_3 = 6 + 1,281$$

$$Q_3 = \underline{7,281}$$

$$Q = \frac{7,281 - 2,779}{2}$$

$$Q = \frac{4,502}{2}$$

$$Q = \underline{2,251}$$

$$M - \sigma = 4,848 - 2,622$$

$$M - \sigma = \underline{2,226}$$



Calculista - (Todos candidatos)

3ª parte

x	T	F	d	Fd	Fd ²	Fa
0-1	 	21	-2	-42	84	21
2-3	 	30	-1	-30	30	51
4-5	 	22	-	-72		73
6-7	 	33	+1	+33	33	106
8-9	 	19	+2	+38	76	125
10	 	6	+3	+18	54	131
		131		+89	277	
				17		

$$M = 5 + \frac{17}{131} \times 2$$

$$\sigma = \pm 2 \sqrt{\frac{277}{131} - 0,130^2}$$

$$M = 5 + 0,130 \times 2$$

$$\sigma = \pm 2 \sqrt{2,114504 - 0,016900}$$

$$M = 5 + 0,260$$

$$\sigma = \pm 2 \sqrt{2,097604}$$

$$M = 5,260$$

$$\sigma = \pm 2 \times 1,448$$

$$\sigma = \pm 2,896$$

$$M_i = 4 + \frac{14,5}{22} \times 2$$

$$M_o = (3 \times 5,318) - (2 \times 5,260)$$

$$M_i = 4 + \frac{29}{22}$$

$$M_o = 15,954 - 10,520$$

$$M_o = 5,434$$

$$M_i = 4 + 1,318$$

$$M_i = 5,318$$

$$P_{15,87} = 0 + \frac{20,7897}{21} \times 2$$

$$P_{84,13} = 8 + \frac{4,2103}{19} \times 2$$

$$P_{15,87} = \frac{41,5794}{21}$$

$$P_{84,13} = 8 + \frac{8,4206}{19}$$

$$P_{15,87} = 1,980$$

$$P_{84,13} = 8 + 0,443$$

$$P_{84,13} = 8,443$$



$$\sigma_{DP} = \frac{2,896}{\sqrt{131 \times 2}}$$

$$\sqrt{131 \times 2}$$

$$\sigma_{DP} = \frac{2,896}{\sqrt{262}}$$

$$\sqrt{262}$$

$$\sigma_{DP} = \frac{2,896}{16,186}$$

$$16,186$$

$$\sigma_{DP} = 0,179$$

$$\sigma_M = \frac{2,896}{\sqrt{131}}$$

$$\sqrt{131}$$

$$\sigma_M = \frac{2,896}{11,445}$$

$$11,445$$

$$\sigma_M = 0,253$$

$$S = \frac{5,260 - 5,434}{2,896}$$

$$2,896$$

$$S = \frac{-0,174}{2,897}$$

$$2,897$$

$$S = -0,060$$

$$CV = \frac{100 \times 2,896}{5,260}$$

$$5,260$$

$$C.V. = \frac{289,6}{5,260}$$

$$5,260$$

$$C.V. = 55,057$$

$$Q_1 = 2 + \frac{11,75 \times 2}{30}$$

$$30$$

$$Q_1 = 2 + \frac{23,50}{30}$$

$$30$$

$$Q_1 = 2 + 0,783$$

$$Q_1 = 2,783$$

$$Q_3 = 6 + \frac{25,25 \times 2}{33}$$

$$33$$

$$Q_3 = 6 + \frac{50,50}{33}$$

$$33$$

$$Q_3 = 6 + 1,530$$

$$Q_3 = 7,530$$

$$Q = \frac{7,530 - 2,783}{2}$$

$$2$$

$$Q = \frac{4,747}{2}$$

$$2$$

$$Q = 0,237$$



Calculista (Todos candidatos)
4ª parte

X	T	F	d	Fd	Fd ²	F ₀
0 - 1		17	-2	-34	68	17
2 - 3		23	-1	-23	23	40
4 - 5		30	-	-57		70
6 - 7		38	+1	+38	38	108
8 - 9		17	+2	+34	68	125
10		6	+3	+18	54	131
		131		+90	251	
				+33		

$$M = 5 + \frac{33}{131} \times 2 \quad M_i = 2 + \frac{48,5 \times 2}{23} \quad M_o = (6,217 \times 3) - (5,504 \times 2)$$

$$M_o = 18,651 - 11,008$$

$$M = 5 + 0,252 \times 2 \quad M_i = 2 + \frac{97}{23} \quad M_o = 7,643$$

$$M = 5 + 0,504 \quad M_i = 2 + 4,217$$

$$M = 5,504 \quad M_i = 6,217 \quad Q_1 = 2 + \frac{15,75 \times 2}{23}$$

$$\sigma = \pm 2\sqrt{\frac{251}{131} - 0,252^2} \quad P_{15,87} = 2 + \frac{3,7897 \times 2}{23} \quad Q_1 = 2 + \frac{31,5}{23}$$

$$\sigma = \pm 2\sqrt{1,916031 - 0,063504} \quad P_{15,87} = 2 + \frac{7,5794}{23} \quad Q_1 = 2 + 1,370$$

$$Q_1 = 3,370$$

$$\sigma = \pm 2\sqrt{1,842527} \quad P_{15,87} = 2 + 0,330$$

$$P_{15,87} = 2,330 \quad Q_3 = 6 + \frac{28,25 \times 2}{38}$$

$$\sigma = \pm 2 \times 1,357$$

$$\sigma = \pm 2,714 \quad P_{84,13} = 8 + \frac{2,2103 \times 2}{17} \quad Q_3 = 6 + \frac{56,5}{38}$$

$$S = \frac{5,504 - 7,643}{2,714} \quad P_{84,13} = 8 + \frac{4,4206}{17} \quad Q_3 = 6 + 1,487$$

$$Q_3 = 7,487$$

$$S = \frac{-2,139}{2,714} \quad P_{84,13} = 8 + 0,260$$

$$S = -0,788 \quad P_{84,13} = 8,260$$



$$Q = \frac{7,487 - 3,370}{2}$$

$$Q = \frac{4,117}{2}$$

$$Q = 2,057$$

$$\sigma_{D.P} = \frac{2,714}{\sqrt{262}}$$

$$\sigma_{D.P} = \frac{2,714}{16,186}$$

$$\sigma_{D.P} = 0,168$$

$$\sigma_M = \frac{2,714}{\sqrt{131}}$$

$$\sigma_M = \frac{2,714}{11,445}$$

$$\sigma_M = 0,237$$

$$C.V = \frac{100 \times 2,714}{5,504}$$

$$C.V = \frac{271,4}{5,504}$$

$$C.V = 49,310$$

$$M.\sigma = 5,504 - 2,714$$

$$M.\sigma = 2,790$$



$$\sigma_{D.P.} = 3,736$$

$$\sqrt{131 \times 2}$$

$$\sigma_{D.P.} = 3,736$$

$$\sqrt{262}$$

$$\sigma_{D.P.} = 2,028$$

$$16,186$$

$$\sigma_{D.P.} = 0,125$$

$$\sigma_M = 3,736$$

$$\sqrt{131}$$

$$\sigma_M = 3,736$$

$$11,445$$

$$\sigma_M = 0,326$$

$$Q_1 = \frac{32,75 \times 2}{75}$$

$$Q_1 = \frac{65,50}{75}$$

$$Q_1 = 0,873$$

$$C.V. = \frac{100 \times 3,736}{7,718}$$

$$C.V. = \frac{373,6}{7,718}$$

$$C.V. = 48,406$$

$$Q_3 = 6 + \frac{7,25 \times 2}{12}$$

$$Q_3 = 6 + \frac{14,50}{12}$$

$$Q_3 = 6 + 1,208$$

$$Q_3 = 7,208$$

$$Q = \frac{7,208 - 0,873}{2}$$

$$Q = \frac{6,335}{2}$$

$$Q = 3,168$$

CALCULISTA
DISTRIBUIÇÃO DE FREQUENCIA (*idade*)



Prova de habilitação Calculista

Candidatos que fizeram a prova de Nível men-
tal e a 2ª parte.

	\mathcal{X}	F	F'	F-F'' = \Delta	
$y_1 = 0,606$	0-4	1	1,63	0,63	N = 127
$y_2 = 1,212$	5-9	7	5,88	1,12	M = 23,485
$y_3 = 1,818$	10-14	10	14,73	4,73	$\sigma = \pm 8,250$
$y_4 = 2,424$	15-19	27	25,55	1,45	$i = 5$
$y_5 = 3,030$	20-24	26	30,70	4,70	$\frac{5}{8,250} = 0,606$
	25-29	26	25,55	0,45	
	30-34	21	14,73	6,27	
	35-39	7	5,88	1,12	$y_0 = \frac{127}{2,507 \times 8,250} \times 5$
	40-44	2	1,63	0,37	$y_0 = 30,70$
	45-49				
	50-54				
		N = 131			

$$y = 0,83225 \times 30,70 = 25,55$$

$$y_1 = 0,47976 \times 30,70 = 14,73$$

$$y_2 = 0,19156 \times 30,70 = 5,88$$

$$y_3 = 0,05299 \times 30,70 = 1,63$$

$$y_4 = 0,01023 \times 30,70 = 0,31$$

y_5

$$\sigma_{F'} = \sqrt{\frac{14,73(127-14,73)}{127}} = \sqrt{\frac{14,73 \times 112,27}{127}} = \sqrt{\frac{1653,7371}{127}} = \sqrt{13,0216} \therefore$$

$$\sigma_{F'} = 3,60$$

$$1 = \frac{6,27}{3,60} = < 3 \text{ não é significativa}$$

CALCULISTA

DISTRIBUIÇÃO DE FREQUENCIA POR IDADE, POR ANO E GLOBAL



Grova de habilitação - Calculista -

Idade

X	F	d	Fd	Fd ²	Fa	
18	12	-5	-60	300	12	
19	17	-4	-68	272	29	$M_i = 21 + \frac{10 \times 1}{12}$
20	25	-3	-75	225	54	
21	12	-2	-24	48	66	$M_i = 21 + \frac{10}{12}$
22	14	-1	-14	14	80	
23	16	-	-24		96	$M_i = 21 + 0,833$
24	9	+1	+9	9	105	$M_i = 21,833$
25	2	+2	+4	8	107	
26	5	+3	+15	45	112	$M_o = (3 \times 21,833) - (2 \times 22,555)$
27	4	+4	+16	64	116	$M_o = 65,449 - 45,110$
28	5	+5	+25	125	121	$M_o = 20,339$
29	2	+6	+12	72	123	
30	1	+7	+7	49	124	
31	4	+8	+32	256	128	
	128		120	1487		
			-121			

$$M = 23,5 - \frac{121}{128} \times 1$$

$$Q_1 = 20 + \frac{3 \times 1}{25}$$

$$M = 23,5 - 0,945$$

$$Q_1 = 20 + 0,12$$

$$M = 22,555$$

$$Q_1 = 20,12$$

$$\sigma = \pm 1 \sqrt{\frac{1487}{128} - 0,945^2}$$

$$Q_3 = 23 + \frac{16 \times 1}{16}$$

$$\sigma = \pm 1 \sqrt{11,617187 - 0,893025}$$

$$Q_3 = 23 + 1$$

$$\sigma = \pm 1 \sqrt{10,724162}$$

$$Q_3 = 24$$

$$\sigma = \pm 1 \times 3,275$$

$$\sigma = \pm 3,275$$



Prova de habilitação

- Calculista -

18 a 19 anos

x	F	d	Fd	Fd ²	Fa
5-9	4	-3	-12	36	4
10-14	2	-2	-4	8	6
15-19	4	-1	-4	4	10
20-24	5	-	-20		15
25-29	8	+1	+8	8	23
30-34	4	+2	+8	16	27
35-39	2	+3	+6	18	29
	29		+22	90	
			2		

$$M = 22,5 + \frac{2}{29} \times 5$$

$$M = 22,5 + 0,069 \times 5$$

$$M = 22,5 + 0,345$$

$$M = 22,845$$

$$\sigma = \pm 5 \sqrt{\frac{90}{29} - 0,069^2}$$

$$\sigma = \pm 5 \sqrt{3,103448 - 0,004761}$$

$$\sigma = \pm 5 \sqrt{3,098687}$$

$$\sigma = \pm 5 \times 1,760$$

$$\sigma = \pm 8,800$$



Prova de habilitação

Calculista

20 a 21 anos

sc	F	d	Fd	Fd ²	Fa
10-14	2	-3	-6	18	2
15-19	9	-2	-18	36	11
20-24	5	-1	-5	5	16
25-29	6	-	-29		22
30-34	10	+1	+10	10	32
35-39	4	+2	+8	16	36
40-44	1	+3	+3	9	37
	37		+21	94	
			-8		

$$M = 27,5 - \frac{8}{37} \times 5$$

$$M = 27,5 - 0,216 \times 5$$

$$M = 27,5 - 1,080$$

$$M = \underline{26,420}$$

$$\sigma = \pm 5 \sqrt{\frac{94}{37} - 0,216^2}$$

$$\sigma = \pm 5 \sqrt{2,540541 - 0,046656}$$

$$\sigma = \pm 5 \sqrt{2,493885}$$

$$\sigma = \pm 5 \times 1,579$$

$$\sigma = \pm \underline{7,895}$$



Prova de habilitação

Calculista

22 a 23 anos

x	F	d	Fd	Fd ²	Fa
0-4	1	-4	-4	16	1
5-9	1	-3	-3	9	2
10-14	2	-2	-4	8	4
15-19	7	-1	-7	7	11
20-24	7	-	-18		18
25-29	7	+1	+7	7	25
30-34	3	+2	+6	12	28
35-39	2	+3	+6	18	30
	30		+19	77	
			+1		

$$M = 22,5 + \frac{1}{30} \times 5$$

$$M = 22,5 + 0,033 \times 5$$

$$M = 22,5 + 0,165$$

$$M = \underline{22,665}$$

$$\sigma = \pm 5 \sqrt{\frac{77}{30} - 0,033^2}$$

$$\sigma = \pm 5 \sqrt{2,566667 - 0,001089}$$

$$\sigma = \pm 5 \sqrt{2,565578}$$

$$\sigma = \pm 5 \times 1,601$$

$$\sigma = \pm \underline{8,005}$$



Prova de habilitação

Calculista

24 a 25 anos

x	F	d	Fd	Fd ²	Fa
5-9	1	-3	-3	9	1
10-14	0	-2			
15-19	3	-1	-3	3	4
20-24	4	-	-6		8
25-29	2	+1	+2	2	10
30-34	1	+2	+2	4	11
	11		+4	18	
			-2		

$$M = 22,5 - \frac{2}{11} \times 5$$

$$M = 22,5 - 0,182 \times 5$$

$$M = 22,5 - 0,910$$

$$M = \underline{21,590}$$

$$\sigma = \pm 5 \sqrt{\frac{18}{11} - 0,182^2}$$

$$\sigma = \pm 5 \sqrt{1,636364 - 0,033124}$$

$$\sigma = \pm 5 \sqrt{1,603240}$$

$$\sigma = \pm 5 \times 1,266$$

$$\sigma = \pm \underline{6,330}$$



Prova de habilitação

Calculista

26 a 27 anos

x_i	F	d	Fd	Fd ²	Fa
10-14	1	-2	-2	4	1
15-19	1	-1	-1	1	2
20-24	4	-	-3		6
25-29	1	+1	+1	1	7
30-34	1	+2	+2	4	8
35-39	0	+3	+0	0	8
40-44	1	+4	+4	16	9
	9		7	26	
			+4		

$$M = 22,5 + \frac{4}{9} \times 5$$

$$M = 22,5 + 0,444 \times 5$$

$$M = 22,5 + 2,220$$

$$M = 24,720$$

$$\sigma = +5 \sqrt{\frac{26}{9}} = 0,4442$$

$$\sigma = +5 \sqrt{2,888889} = 0,197163$$

$$\sigma = +5 \sqrt{2,691726}$$

$$\sigma = +5 \times 1,641$$

$$\sigma = +8,205$$



Prova de habilitação

Calculista

28 a 29 anos

De	F	d	Fd	Fd ²	Fa
5-9	1	-2	-2	4	1
10-14	2	-1	-2	2	3
15-19	2	-	-4		5
20-24	0	+1			
25-29	1	+2	+2	4	6
30-34	1	+3	+3	9	7
	7		+5	19	
			+1		

$$M = 17,5 + \frac{1}{7} \times 5$$

$$M = 17,5 + 0,143 \times 5$$

$$M = 17,5 + 0,715$$

$$M = \underline{18,215}$$

$$\sigma = \pm 5 \sqrt{\frac{19}{7} - 0,143^2}$$

$$\sigma = \pm 5 \sqrt{2,714286 - 0,020449}$$

$$\sigma = \pm 5 \sqrt{2,693837}$$

$$\sigma = \pm 5 \times 1,641$$

$$\sigma = \pm \underline{8,207}$$



Prova de habilitação

Calculista

30 a 31 anos

x_c	F	d	Fd	Fd ²	Fa
5-9	1	-2	-2	4	1
10-14	1	-1	-1	1	2
15-19	0	-	-3		2
20-24	2	+1	+2	2	4
25-29	1	+2	+2	4	5
	5		+4	11	
			1		

$$M = 17,5 + \frac{1}{5} \times 5$$

$$M = 17,5 + 0,2 \times 5$$

$$M = 17,5 + 1$$

$$M = 18,5$$

$$\sigma = \pm 5 \sqrt{\frac{11}{5} - 0,2^2}$$

$$\sigma = \pm 5 \sqrt{2,2 - 0,04}$$

$$\sigma = \pm 5 \sqrt{2,16}$$

$$\sigma = \pm 5 \times 1,4$$

$$\sigma = \pm 7$$

CALCULISTA

CALCULOS PARA AJUSTAMENTO DA CURVA/



Prova de habilitação

Calculista
Curva ajustada

X	f	f'	$ f-f' =\Delta$	
0 - 4	1	1,76	0,76	$N = 131$
5 - 9	8	6,20	1,80	
10 - 14	10	15,25	5,25	$M = 23,49$
15 - 19	27	26,17	0,83	
20 - 24	27	31,33	4,33	$\sigma = \pm 8,34$
25 - 29	27	26,17	0,83	
30 - 34	21	15,25	5,75	$i = 5$
35 - 39	8	6,20	1,80	
40 - 44	2	1,76	0,24	$\frac{i}{\sigma} = \frac{5}{8,34} = 0,600$
45 - 47				

131

$$y_1 = 0,600 \sigma$$

$$y_2 = 1,200 \sigma$$

$$y_3 = 1,800 \sigma$$

$$y_4 = 2,400 \sigma$$

$$y_5 = 3,000 \sigma$$

$$y_0 = \frac{131}{2,507 \times 8,34} \times 5 = 31,33$$

$$y_1 = 0,83527 \times 31,33 = 26,17$$

$$y_2 = 0,48675 \times 31,33 = 15,25$$

$$y_3 = 0,19790 \times 31,33 = 6,20$$

$$y_4 = 0,05614 \times 31,33 = 1,76$$

$$y_5 = 0,01111 \times 31,33 = 0,35$$



$$\sigma_{f'} = \sqrt{\frac{15,25(131 - 15,25)}{131}} = \sqrt{\frac{15,25 \times 115,75}{131}}$$

$$\sigma_{f'} = \sqrt{\frac{1765,1875}{131}} = \sqrt{13,474714}$$

$$\sigma_{f'} = 3,671$$

$$\frac{\Delta}{\sigma_{f'}} = \frac{5,75}{3,671} < 3 \text{ não é significativa}$$

$$\sigma_{f''} = \sqrt{\frac{31,33(131 - 31,33)}{131}} = \sqrt{\frac{31,33 \times 99,67}{131}}$$

$$\sigma_{f''} = \sqrt{\frac{3122,10611}{131}} = \sqrt{23,837108}$$

$$\sigma_{f''} = 4,882$$

$$\frac{\Delta}{\sigma_{f''}} = \frac{4,33}{4,882} < 3 \text{ não é significativa}$$



Polimento por per-equação
 Prova de habilitação de balcista

X	f	f ₁ '	f ₂ '	f ₃ '
-15 - -19				0,04
-10 - -14			0,11	0,37
-5 - -9		0,33	1,00	1,37
0 - 4	1	2,67	3,00	3,93
5 - 9	7	6,00	7,78	8,22
10 - 14	10	14,67	13,89	14,11
15 - 19	27	21,00	20,67	19,48
20 - 24	26	26,33	23,89	22,48
25 - 29	26	24,33	22,89	21,41
30 - 34	21	18,00	17,44	16,89
35 - 39	7	10,00	10,33	10,78
40 - 44	2	3,00	4,56	5,37
45 - 49		0,67	1,22	2,00
50 - 54			0,22	0,47
55 - 60				0,07
	$\Sigma f = 127$	$\Sigma f_1' = 127,00$	$\Sigma f_2' = 127,00$	$\Sigma f_3' = 126,99$

$$\sigma_{f_3} = \sqrt{\frac{19(27-19)}{127}} = \sqrt{\frac{19 \times 108}{127}} = \sqrt{\frac{2025}{127}}$$

$$\sigma_{f_3} = 4,020$$

$$\frac{27-19}{4,020} = \frac{8}{4,020} = 1,99 \text{ não é significativa}$$

$$\sigma_{f_2} = \sqrt{\frac{22(127-22)}{127}} = \sqrt{\frac{22 \times 105}{127}} = \sqrt{\frac{2310}{127}} = 3,212$$

$$\frac{26-22}{3,212} = 1,24 \text{ não é significativa}$$

CALCULISTA

COCORRELAÇÃO

Prova de habilitação

Calculista

VARIÁVEL Y

	18	19	20	21	22	23	24	25	26	27	28	29	30	31	f	d	fd	fd ²
0-9		10	12		8		4								5	-4	-20	80
10	60	36	18		3		3		9				21	24	14	-3	-42	126
20	20	12	24	4	10		2		136		20	12		16	19	-2	-38	76
30	10	4	9	2	2		2	2	8	5				8	18	-1	-18	18
40															17	-	-118	
50	16	9	6		2										12	+1	+12	12
60	22	2	8		5	3	6		6		12				12	+2	+24	48
70	45	2	5	6	8		3		12	1					16	+3	+48	144
80		32	12	8	4					16		24			7	+1	+28	112
90								20	25						3	+5	+15	75
100			12												1	+0	+0	36
f	12	16	25	11	14	14	9	2	5	4	5	2	1	4	124	$\frac{+133}{+15}$	727	
d	-5	-4	-3	-2	-1	-	+1	+2	+3	+4	+5	+6	+7	+8				
fd	-60	-64	-75	-22	-14	-235	+9	+4	+15	+16	+25	+12	+7	+32	$\frac{+120}{-115}$			
fd ²	300	256	225	44	14		9	8	45	64	125	72	49	256	1467			

Idade Y

2ª Parte X

VARIÁVEL Y	VARIÁVEL X	Coefficiente de Correlação	Intercepto
M = 23,5	M = 45 + $\frac{15}{127} \times 10$	$r = \frac{115 - (23,5 \times 127)}{3,312 \times 24,18}$	$r = \frac{1 - 0,2218}{\sqrt{0,24}}$
M = 23,5	M = 45 + 0,121 \times 10	$r = \frac{115 - (23,5 \times 127)}{3,312 \times 24,18}$	$r = \frac{1 - 0,2218}{\sqrt{0,24}}$
M = 22,573	M = 45 + 1,21	$r = \frac{115 - (22,573 \times 127)}{3,312 \times 24,18}$	$r = \frac{1 - 0,2218}{\sqrt{0,24}}$
$\sigma = \sqrt{\frac{1467}{124} - 0,727^2}$	M = 16,21	$r = \frac{115 - (16,21 \times 127)}{3,312 \times 24,18}$	$r = \frac{1 - 0,2218}{\sqrt{0,24}}$
$\sigma = \sqrt{12,771316}$	$\sigma = 10 \sqrt{\frac{1467}{124} - 0,727^2}$	$r = 0,0039 \times 10$	$r = 0,039$
$\sigma = 3,312$	$\sigma = 10 \sqrt{12,771316}$	$r = 0,24$	
	$\sigma = 10 \sqrt{12,771316}$		
	$\sigma = 10 \times 2,917$		
	$\sigma = 29,18$		

Grova de habilitação

Calculista

mat.
VARIÁVEL X

	0-4	5-9	10-14	15-19	20-24	25-29	30-34	35-39	40	f	d	fd	fd²
0-4	45	30	10				20			12	-5	-60	300
5-9	32	28	4	20		8	16			18	-4	-72	288
10-14	36	25	30	6		3	8			14	-3	-42	126
15-19	8	20	4			16	6	8		20	-2	-40	80
20-24		2			5	2	3			12	-1	-12	12
25-29										4		-226	
30-34		2			2	2	3			5	+1	+5	5
35-39		4	2		2	4	6			6	+2	+12	24
40-44	-4	3			6	2	18			7	+3	+21	63
45-49		8			4	8	12			7	+4	+28	112
50-54		10	5		5	10	15			9	+5	+45	225
55-59					6	36	36			11	+6	+66	396
60						14	28			2	+7	+14	98
f	6	4	23	15	34	15	19	9	2	127		+194	1729
d	-4	-3	-2	-1		+1	+2	+3	+4				
fd	-24	-12	-46	-15	-97	+15	+38	+27	+8			+88	
fd²	96	36	92	15		15	76	81	32			443	

Matemática - X

Estatística - Y

Variável X	Variável Y	Coefficiente de Correlação	Erro Padrão da Correlação
$M = 22,5 - \frac{9}{127} \times 5$	$M = 27,5 - \frac{35}{127} \times 5$	$r = \frac{372 - (0,071 \times 0,276) \times 5 \times 5}{9,330 \times 18,395}$	$\sigma_r = \frac{1 - 0,425^2}{\sqrt{127}}$
$M = 22,5 - 0,071 \times 5$	$M = 27,5 - 0,276 \times 5$	$r = \frac{2929134 - 0,019596 \times 25}{171,625350}$	$\sigma_r = \frac{1 - 0,178500}{11,269}$
$M = 22,5 - 0,355$	$M = 27,5 - 1,380$	$r = \frac{2,909538}{171,625350} \times 25$	$\sigma_r = \frac{0,821500}{11,269}$
$M = 22,145$	$M = 26,120$	$r = 0,017 \times 25$	$\sigma_r = 0,073$
$\sigma = \pm 5 \sqrt{\frac{443}{127} - 0,071^2}$	$\sigma = \pm 5 \sqrt{\frac{1729}{127} - 0,276^2}$	$r = 0,425$	
$\sigma = \pm 5 \sqrt{3,488189 - 0,005041}$	$\sigma = \pm 5 \sqrt{13,614173 - 0,076176}$		
$\sigma = \pm 5 \sqrt{3,483148}$	$\sigma = \pm 5 \sqrt{13,537997}$		
$\sigma = \pm 5 \times 1,866$	$\sigma = \pm 5 \times 3,679$		
$\sigma = \pm 9,330$	$\sigma = \pm 18,395$		

VARIÁVEL Y

$\Sigma(y \cdot x)$
372

Calculista

(P.H. INEP. S.A. MT.)

Nivel mental x Matemática

$$N = 127$$

$$P = 0,48$$

$$\sigma_r = \pm 0,068$$

Rio, 6/2/1943.

Prova de habilitação

Candidatos do Distrito Federal

VARIÁVEL X **Calculista**

Nível mental X

Matemática Y

VARIÁVEL Y

	0-4	5-9	10-14	15-19	20-24	25-29	30-34	35-39	40-44	45-47	f _i	d	f _d	f _d ²
0-4	16	36	8	4							6	-4	-24	96
5-9		119	3								4	-3	-12	36
10-14		6	16	12							23	-2	-46	92
15-19		6	2	4							15	-1	-15	15
20-24											34		-97	
25-29											15	1	15	15
30-34											19	2	38	76
35-39											9	3	27	81
40											2	4	8	32
F	1	7	10	27	26	26	21	7	2		127		88	443
d	-4	-3	-2	-1		1	2	3	4					
f _d	-4	-21	-20	-27	-72	26	42	21	8				+97	
f _d ²	16	63	40	27		26	84	63	32				+25	
Σ f _d														
Σ f _d ²														185

VARIÁVEL X	VARIÁVEL Y	Coefficiente de Correlação r	Erro Padrão da Correlação
M = $22,5 + \frac{25}{127} \times 5$	M = $22,5 - \frac{9}{127} \times 5$	$r = \frac{127 + (0,197 \times 2011) \times 5 \times 5}{8250 \times 9,330}$	$\sigma_r = \pm \frac{1 - 0,49^2}{\sqrt{127}}$
M = $22,5 + 0,197 \times 5$	M = $22,5 - 0,071 \times 5$	$r = \frac{1457 - (0,197 \times 7) \times 25}{76,97 \times 2500}$	$\sigma_r = \pm \frac{0,7696}{11,269}$
M = $22,5 + 0,985$	M = $22,5 - 0,355$	$r = \frac{1457 + 0,013787 \times 25}{76,97 \times 2500}$	$\sigma_r = \pm 0,068$
M = $23,485$	M = $22,145$		
$\sigma = \pm 5 \sqrt{\frac{351}{127} - 0,197^2}$	$\sigma = \pm 5 \sqrt{\frac{443}{127} - 0,071^2}$	$r = \frac{1470937 \times 9,5}{76,97 \times 2500}$	
$\sigma = \pm 5 \sqrt{2,763780 - 0,038809}$	$\sigma = \pm 5 \sqrt{3,483189 - 0,005044}$	$r = \frac{1470997 \times 25}{76,97 \times 2500}$	
$\sigma = \pm 5 \sqrt{2,724971}$	$\sigma = \pm 5 \sqrt{3,483148}$	$r = 0,019 \times 25$	
$\sigma = \pm 5 \times 1,650$	$\sigma = \pm 5 \times 1,866$	$r = 0,475 \therefore r = 0,49$	
$\sigma = \pm 8,250$	$\sigma = \pm 9,330$		

VARIÁVEL X	VARIÁVEL Y	Coeficiente de Correlação	Exatidão da Correlação
------------	------------	---------------------------	------------------------

$$M = 22,5 + \frac{24}{128} \times 5$$

$$M = 22,5 + 0,188 \times 5$$

$$M = 22,5 + 0,940$$

$$M = 23,440$$

$$\sigma = \pm \sqrt{\frac{364}{128} - 0,188^2}$$

$$\sigma = \pm \sqrt{2,843750 - 0,035344}$$

$$\sigma = \pm \sqrt{2,808406}$$

$$\sigma = \pm 1,676$$

$$\sigma = \pm 1,676$$

$$M = 23,5 - \frac{121}{128} \times 1$$

$$M = 23,5 - 0,945$$

$$M = 22,555$$

$$\sigma = \pm \sqrt{\frac{1487}{128} - 0,945^2}$$

$$\sigma = \pm \sqrt{11,617187 - 0,893025}$$

$$\sigma = \pm \sqrt{10,724162}$$

$$\sigma = \pm 3,275$$

$$\sigma = \pm 3,275$$

$$r = \frac{\frac{127}{128} - (0,188 \times 0,945)}{8,380 \times 3,275} \times 5 \times 1$$

$$r = \frac{-0,992188 - (0,177660)}{27,444500} \times 5$$

$$r = \frac{-0,814528}{27,444500} \times 5$$

$$r = -0,030 \times 5$$

$$r = -0,150$$

$$\sigma_r = \frac{1 - 0,150^2}{\sqrt{128}}$$

$$\sigma_r = \frac{1 - 0,022500}{11,313708}$$

$$\sigma_r = \frac{0,977500}{11,313708}$$

$$\sigma_r = 0,086$$

Calculista

(P.H. - INEP S.A. - MT.)

Nível mental x Estatística

$$N = 127$$

$$r = 0,38$$

$$\sigma_r = \pm 0,0124$$

Rio, 23/2/1943.

Grova de habilitação

Calculista

Nível mental X
Estatística Y

VARIÁVEL X

VARIÁVEL Y

	0-4	5-9	10-14	15-19	20-24	25-29	30-34	35-39	40-44	45-49	Σf	d	$f \cdot d$	$\frac{f \cdot d}{\Sigma f}$
0-4		15		20		10					12	-5	-60	300
5-9		24	24	20		12	24				18	-4	-72	288
10-14	12	9	6	15		6	6	9			14	-3	-42	126
15-19		12	8	8		8	16				20	-2	-40	80
20-24			2	2		4	2	3			12	-1	-12	12
25-29											4		-226	
30-34			2				2	6			5	1	5	5
35-39		6		6		2	4				6	2	12	24
40-44			6				6				7	3	21	63
45-49				8		8	8	25			7	4	28	112
50-54		10				20	30				9	5	45	225
55-59				12		12	24	36	48		11	6	66	396
60							14	21			2	7	14	98
Σf	1	7	10	27	26	26	21	7	2		127		191	1729
d	-4	-3	-2	-1		1	2	3	4				-35	
$f \cdot d$	-4	-21	-20	-27	-72	26	42	21	8				-97	+25
$f \cdot d^2$	16	63	40	27		26	84	63	32				351	

$\Sigma(x \cdot y) = 289$

VARIÁVEL X	VARIÁVEL Y	Coefficiente de Correlação	Erro Padrão da Correlação
$M = 22,5 + \frac{25}{127} \times 5$	$M = 27,5 - \frac{35}{127} \times 5$	$r = \frac{289 - (0,197 \times 0,276)}{8,250 \times 18,395} \times 5 \times 5$	$\sigma_r = \pm \frac{1 - 0,375^2}{\sqrt{127}}$
$M = 22,5 + 0,197 \times 5$	$M = 27,5 - 0,276 \times 5$		
$M = 22,5 + 0,985$	$M = 27,5 - 1,380$	$r = \frac{2,275 - (0,054372)}{151,758750} \times 25$	$\sigma_r = \pm \frac{0,40625}{11,269}$
$M = 23,485$	$M = 26,120$	$r = \frac{2,329372}{151,758750} \times 25$	$\sigma_r = \pm 0,0124$
$\sigma = \pm 5 \sqrt{\frac{351}{127} - 0,197^2}$	$\sigma = \pm 5 \sqrt{\frac{1729}{127} - 0,276^2}$	$r = 0,015 \times 25$	
$\sigma = \pm 5 \sqrt{2,763780 - 0,038809}$	$\sigma = \pm 5 \sqrt{13,614173 - 0,076176}$	$r = 0,375 \therefore r = 0,38$	
$\sigma = \pm 5 \sqrt{2,724971}$	$\sigma = \pm 5 \sqrt{13,537997}$		
$\sigma = \pm 5 \times 1,650$	$\sigma = \pm 5 \times 3,679$		
$\sigma = \pm 8,250$	$\sigma = \pm 18,395$		

Prova de habilitação Calculista

VARIÁVEL X

NÍVEL MENTAL X
2ª PARTE Y

	0	5	10	15	20	25	30	35	40	45	f	d	fd	fd²
	4	9	14	19	24	29	34	39	44	49				
0-9		12	8	4	4						5	-4	-20	80
10-19	12	18	14	9	4	4	12				14	-3	-42	126
20-29		12	12	10	5	10	4				20	-2	-40	80
30-39		3	2	6	5	3	8				20	-1	-20	20
40-49											17	-	-	-
50-59		3	2	3	2	2	2	6			12	1	12	12
60-69		2	4	3	3	6	8	6			12	2	24	48
70-79			3	9	4	2	4	12			16	3	48	144
80-89					4	16	3	24			7	4	28	122
90-99						1	10	15	20		3	5	15	75
100							1	18			1	6	6	36
f	1	7	10	27	26	26	21	7	2	-	127		11	733
d	-4	-3	-2	-1	-	1	2	3	4	5				
fd	-4	-21	-20	-27	-	26	42	21	8	-	25			
fd²	16	63	40	27	-	26	84	63	32	-	351			

VARIÁVEL X	VARIÁVEL Y	CORRELAÇÃO	ERRO DA CORRELAÇÃO
$M = 22,5 + \frac{25}{127} \times 5$	$M = 45 + \frac{11}{127} \times 10$	$r = \frac{238}{127} - \frac{0,197 \times 0,086}{1,65 \times 2,4009}$	$\sigma_r = 1 - \frac{(0,469)^2}{\sqrt{127}}$
$M = 22,5 + 0,197 \times 5$	$M = 45 + 0,0866 \times 10$	$r = \frac{18740157 - 0,0170602}{3,961485}$	$\sigma_r = 1 - \frac{0,219961}{11,269}$
$M = 22,5 + 0,985$	$M = 45,866$	$r = \frac{1,8569555}{3,961485}$	$\sigma_r = \frac{0,780039}{11,269}$
$M = 23,485$			
$\sigma = \pm 5 \sqrt{\frac{351}{127} - 0,197^2}$	$\sigma = \pm 10 \sqrt{\frac{733}{127} - 0,0866^2}$	$r = 0,469$	$\sigma_r = 0,0692$
$\sigma = \pm 5 \sqrt{2,763780 - 0,038809}$	$\sigma = \pm 10 \sqrt{5,77165354 - 0,00749956}$		
$\sigma = \pm 5 \sqrt{2,724971}$	$\sigma = \pm 10 \sqrt{5,76415398}$		
$\sigma = \pm 5 \times 1,650$	$\sigma = \pm 10 \times 2,4009$		
$\sigma = \pm 8,250$	$\sigma = \pm 24,009$		

VARIÁVEL Y

Grova de habilitação

Calculista

Idade X
Matemática Y

VARIÁVEL X

	18	19	20	21	22	23	24	25	26	27	28	29	30	31	f	d	fd	fd ²	
0-4	2 ¹	3 ²			8 ²		4 ¹								6	-4	-24	36	
5-9					3 ¹		3 ¹								4	-3	-12	36	
10-14	4 ⁴	2 ³	2 ⁴	2 ⁴	8 ³	6 ³	2 ¹		3 ³						23	-2	-46	92	
15-19	5 ¹	3 ³	1 ²	3 ¹	3 ³		2 ²			2 ²	1 ¹⁰	6 ¹	7 ¹		15	-1	-15	15	
20-24	3 ³	3 ³	1 ¹	3 ³	2 ²	4 ¹				2 ²	1 ¹	1 ¹			31	-	-37		
25-29	3 ³	1 ³	1 ²	3 ³	2 ²	3 ²	2 ²		1 ³						15	-1	-15	15	
30-34		1 ²	3 ³	2 ²	1 ²	2 ²	4 ²	8 ²	6 ¹						2	19	+2	38	76
35-39			1 ²	3 ³	1 ²					2 ²	2 ⁴				9	-3	-27	81	
40			1 ¹	1 ²	8 ³										2	-4	-8	32	
f	12	16	25	11	14	14	9	2	5	4	5	2	1	4	124		+88	443	
d	-5	-4	-3	-2	-1	-	+1	+2	+3	+4	+5	+6	+7	+8					
fd	-60	-64	-75	-22	-14	-235	9	8	15	16	25	12	7	32			+120	-115	
fd ²	300	256	225	44	14		9	16	45	64	125	72	49	256	1467				

Variável X	Variável Y	Coefficiente de correlação	Erro padrão de correlação
$M = 23,5 - \frac{115}{124}$	$M = 22,5 - \frac{9}{124} \times 5$	$r = \frac{77}{124} - (0,927 \times 0,073) \times 5$	$\sigma_r = \frac{1 - 0,090^2}{\sqrt{124}}$
$M = 23,5 - 0,927$	$M = 22,5 - 0,073 \times 5$	$r = \frac{0,637097 - (0,067671) \times 5}{31,281740}$	$\sigma_r = \frac{1 - 0,008100}{11,136}$
$M = 22,573$	$M = 22,5 - 0,365$	$r = \frac{0,569426}{31,281740} \times 5$	$\sigma_r = \frac{0,991800}{11,136}$
$\sigma = \pm \sqrt{\frac{1467}{124} - 0,927^2}$	$M = 22,135$	$r = 0,018 \times 5$	$\sigma_r = 0,089$
$\sigma = \pm \sqrt{1,830645 - 0,85205}$	$\sigma = \pm 5 \sqrt{3,988119 - 0,00522}$	$r = 0,090$	
$\sigma = \pm \sqrt{10,971316}$	$\sigma = \pm 5 \sqrt{3,567252}$		
$\sigma = \pm 3,312$	$\sigma = \pm 5 \times 1,889$		
	$\sigma = \pm 9,445$		

VARIÁVEL Y

$\Sigma(yx)$
+73

CALCULISTA

**DISTRIBUIÇÃO DE FREQUENCIA (Matemática e Estatística, Nivel
Mental)**



Prova de habilitação

Calculista

Candidatos que fizeram a prova de nível
muita e a 2ª parte.

X	T	F	a	Fa	Fa ²	Fa
0-4	I	1	-4	-4	16	1
5-9	IIII	7	-3	-21	63	8
10-14	IIIIII	10	-2	-20	40	18
15-19	IIIIIIIIII	27	-1	-27	27	45
20-24	IIIIIIIIIIII	26	-	-72		71
25-29	IIIIIIIIIIIIII	26	1	26	26	97
30-34	IIIIIIIIIIIIIIII	21	2	42	84	118
35-39	IIIIIIIIII	7	3	21	63	125
40-44	IIIIIIII	2	4	8	32	127
45-47				+37	351	
		127		+25		

$$M = 22,5 + \frac{25}{127} \times 5 \quad \sigma = \pm 5 \sqrt{\frac{351}{127}} = 0,197^2$$

$$M = 22,5 + 0,197 \times 5 \quad \sigma = \pm 5 \sqrt{2,763780} = 0,038809$$

$$M = 22,5 + 0,985 \quad \sigma = \pm 5 \sqrt{2,724971}$$

$$M = 23,485 \quad \sigma = \pm 5 \times 1,650$$

$$M_i = 20 + \frac{18,5 \times 5}{26} \quad \sigma = \pm 8,250$$

$$M_i = 20 + \frac{92,5}{26}$$

$$M_i = 20 + 3,558 \therefore M_i = 23,558$$

$$P_{15,87} = 15 + \frac{2,1549 \times 5}{27}$$

$$P_{15,87} = 15 + \frac{10,7945}{27}$$

$$P_{15,87} = 15 + 0,40$$

$$P_{15,87} = 15,40.$$

$$P_{13,84} = 10 + \frac{9,5768 \times 5}{10}$$

$$P_{13,84} = 10 + \frac{47,8840}{10}$$

$$P_{13,84} = 10 + 4,78840$$

$$P_{13,84} = 14,788$$



$$M_0 = (3 \times 23,558) - (2 \times 23,485)$$

$$S = \frac{23,485 - 23,704}{8,250}$$

$$M_0 = 70,674 - 46,970$$

$$S = \frac{-0,219}{8,250}$$

$$M_0 = 23,704$$

$$S = -0,027$$

$$\sigma_{D.P.} = \frac{8,250}{\sqrt{127 \times 2}}$$

$$C.V. = \frac{100 \times 8,250}{23,485} =$$

$$\sigma_{D.P.} = \frac{8,250}{\sqrt{254}}$$

$$C.V. = \frac{825}{23,485}$$

$$\sigma_{D.P.} = \frac{8,250}{\sqrt{15,937}}$$

$$C.V. = 35,129$$

$$\sigma_{D.P.} = 0,518$$

$$Q_1 = 15 + \frac{13,75 \times 5}{27}$$

$$\sigma_M = \frac{8,250}{\sqrt{127}}$$

$$Q_1 = 15 + \frac{68,75}{27}$$

$$Q_1 = 15 + 2,546$$

$$\sigma_M = \frac{8,250}{11,269}$$

$$Q_1 = 17,546$$

$$\sigma_M = 0,732$$

$$Q_3 = 25 + \frac{24,25 \times 5}{26}$$

$$Q = \frac{29,667 - 17,546}{2}$$

$$Q_3 = 25 + \frac{121,25}{26}$$

$$Q = \frac{12,121}{2}$$

$$Q_3 = 25 + 4,667$$

$$Q = 6,061$$

$$Q_3 = 29,667$$



Prova de habilitação

Nível Fundamental

Calculista

X	F	d	Fd	Fd ²	Fa	
0-4	1	-4	-4	16	1	
5-9	8	-3	-24	72	9	$Mi = 20 + \frac{19 \times 5}{27}$
10-14	10	-2	-20	40	19	
15-19	26	-1	-26	26	45	$Mi = 20 + \frac{95}{27}$
20-24	27	-	-74		72	
25-29	26	1	26	26	98	$Mi = 20 + 3,519$
30-34	20	2	40	80	118	
35-39	8	3	24	72	126	$Mi = 23,519$
40-44	2	4	8	32	128	
45-47						
	128		98	364		
			24			

$$M = 22,5 + \frac{24 \times 5}{128}$$

$$M = 22,5 + 0,188 \times 5$$

$$M = 22,5 + 0,940$$

$$M = 23,440$$

$$\sigma = \pm 5 \sqrt{\frac{364}{128} - 0,188^2}$$

$$\sigma = \pm 5 \sqrt{2,843750 - 0,035344}$$

$$\sigma = \pm 5 \sqrt{2,808406}$$

$$\sigma = \pm 5 \times 1,676$$

$$\sigma = \pm 8,380$$



Prova de habilitação

Calculista

Aritmética

X	T	F	d	F _d	F _{d2}
0-4	IIII	6	4	-24	96
5-9	IIII	4	3	-12	36
10-14	IIII IIII	23	2	-46	92
15-19	IIII IIII	15	1	-15	15
20-24	IIII IIII IIII	34		-97	
25-29	IIII IIII	15	1	15	15
30-34	IIII IIII IIII	19	2	38	76
35-39	IIII IIII	9	3	27	81
40	II	2	4	8	32
		127		+88	443
				-9	

$$M = 22,5 \frac{9}{127} \times 5$$

$$\sigma = +5 \sqrt{\frac{443}{127}} = 0,0712$$

$$M = 22,5 - 0,071 \times 5$$

$$\sigma = +5 \sqrt{3,488189} = 0,005041$$

$$M = 22,5 - 0,355$$

$$\sigma = +5 \sqrt{3,483148}$$

$$M = 22,145$$

$$\sigma = +5 \times 1,866$$

$$\sigma = +9,330$$



Prova de habilitação

Calculista

Estatística

x	T	F	d	Fd	Fd ²	Fa
0-4		12	5	60	300	12
5-9		18	4	72	288	30
10-14		14	3	42	126	44
15-19		20	2	40	80	64
20-24		12	1	12	12	76
25-29		4	—	—	—	80
30-34		5	1	5	5	85
35-39		6	2	12	24	91
40-44		7	3	21	63	98
45-49		7	4	28	112	105
50-54		9	5	45	225	114
55-59		11	6	66	396	125
60		2	7	14	98	127
		127		191	1729	
				-35		

$$M = 27,5 - \frac{35}{127} \times 5$$

$$\sigma = +5 \sqrt{\frac{1729}{127} - 0,276^2}$$

$$M = 27,5 - 0,276 \times 5$$

$$\sigma = +5 \sqrt{13,614123 - 0,076176}$$

$$M = 27,5 - 1,380$$

$$\sigma = +5 \sqrt{13,537997}$$

$$M = 26,120$$

$$\sigma = +5 \times 3,679$$

$$\sigma = +18,395$$



Prova de habilitação

Calculista

2ª parte

0-9		5	-	4	-	20	180	5
10-19		14	-	3	-	42	126	19
20-29		20	-	2	-	40	80	39
30-39		20	-	1	-	20	20	59
40-49		17	-		-	122		76
50-59		12		1		12	12	88
60-69		12		2		24	48	100
70-79		16		3		48	144	116
80-89		7		4		28	112	123
90-99		3		5		15	75	126
100		1		6		6	36	127
		127				133	733	
						+ 11		

$$M = 45 + \frac{11}{127} \times 10$$

$$\sigma = \pm 10 \sqrt{\frac{733}{127} - 0,0866^2}$$

$$M = 45 + 0,0866 \times 10$$

$$\sigma = \pm 10 \sqrt{5,77165354 - 0,00749956}$$

$$45 + 0,866$$

$$\sigma = \pm 10 \sqrt{5,76415398}$$

$$45,866$$

$$\sigma = \pm 10 \times 2,4009$$

$$\sigma = \pm 24,009$$



Prova de Habilitação

Calculista

Idade

(Candidatos que fizeram a 2ª parte)

X	f	a	fd	fd ²	fa
18	12	-5	-60	300	
19	16	-4	-64	256	
20	25	-3	-75	225	
21	11	-2	-22	44	
22	14	-1	-14	14	
23	14		-235		
24	9	1	9	9	
25	2	2	4	8	
26	5	3	15	45	
27	4	4	16	64	
28	5	5	25	125	
29	2	6	12	72	
30	1	7	7	49	
31	4	8	32	256	
	124		120	1467	
			-115		

$$M = 23,5 - \frac{115}{124}$$

$$\sigma = \pm \sqrt{\frac{1467}{124} - 0,9272}$$

$$M = 23,5 - 0,927$$

$$\sigma = \pm \sqrt{11,830645 - 0,859329}$$

$$M = 22,573$$

$$\sigma = \pm \sqrt{10,971316}$$

$$\sigma = \pm 3,312$$



Prova de habilitação

Calculista

(Candidatos que declararam a idade)
Estatística

x	F	d	Fd	Fd ²
0-4	12	-5	-60	300
5-9	17	-4	-68	272
10-14	13	-3	-39	117
15-19	19	-2	-38	76
20-24	12	-1	-12	12
25-29	4	-	-217	
30-34	5	1	5	5
35-39	6	2	12	24
40-4	7	3	21	63
45	7	4	28	112
50	9	5	45	225
55	11	6	66	396
60	2	7	14	98
	124		191	1700
			-26	

$$M = 27,5 - \frac{26}{124} \times 5$$

$$\sigma = +5 \sqrt{\frac{1700}{124} - 0,210^2}$$

$$\sigma = +5 \sqrt{13,709677 - 0,044100}$$

$$M = 27,5 - 0,210 \times 5$$

$$\sigma = +5 \sqrt{13,665577}$$

$$M = 27,5 - 1,050$$

$$\sigma = +5 \times 3,697$$

$$M = 26,450$$

$$\sigma = +18,485$$



Prova de habilitação

Calculista

- 2ª parte -

(Candidatos que declararam a idade)

X	f	a	fa	fa ²	fa ³
0 - 9	5	-4	-20	80	5
10 - 19	14	-3	-42	126	19
20 - 29	19	-2	-38	76	38
30 - 39	18	-1	-18	18	56
40 - 49	17		-18		73
50 - 59	12	1	12	12	85
60 - 69	12	2	24	48	97
70 - 79	16	3	48	144	113
80 - 89	7	4	28	112	120
90 - 99	3	5	15	75	123
100	1	6	6	36	124
	124		133	727	
			+15		

$$M = 45 + \frac{15}{124} \times 10$$

$$\sigma = \pm 10 \sqrt{\frac{727}{124} - 0,121^2}$$

$$M = 45 + 0,121 \times 10$$

$$\sigma = \pm 10 \sqrt{5,862903 - 0,014641}$$

$$M = 45 + 1,21$$

$$\sigma = \pm 10 \sqrt{5,848262}$$

$$M = 46,21$$

$$\sigma = \pm 10 \times 2,418$$

$$\sigma = \pm 24,18$$



Prova de habilitação

Calculista

Matemática

(Candidatos que declararam a idade)

0 - 4	6	- 4	- 24	96
5 - 9	4	- 3	- 12	36
10 - 14	23	- 2	- 46	92
15 - 19	15	- 1	- 15	15
20 - 24	31	—	- 97	
25 - 29	15	1	15	15
30 - 34	19	2	38	76
35 - 39	9	3	27	81
40	2	4	8	32
	124		88	443
			- 9	

$$M = 22,5 - \frac{9}{124} \times 5 \quad \sigma = \pm 5 \sqrt{\frac{443}{124}} - 0,073$$

$$M = 22,5 - 0,073 \times 5 \quad \sigma = \pm 5 \sqrt{3,572581} - 0,005329$$

$$M = 22,5 - 0,365 \quad \sigma = \pm 5 \sqrt{3,567252}$$

$$M = 22,135 \quad \sigma = \pm 5 \times 1,889$$

$$\sigma = \pm 9,445$$

CALCULISTA

CRESCIMENTO DA MEDIA POR IDADE.

NIVEL MENTAL



MINISTÉRIO DA EDUCAÇÃO E SAÚDE

INSTITUTO NACIONAL DE ESTUDOS PEDAGÓGICOS

Prova de habilitação

— Calculista —

nível mental

Idades	N	Normas	
		M	σ
18 - 19	29	22,845	8,800
20 - 21	37	26,420	7,895
22 - 23	30	22,665	8,005
24 - 25	11	21,590	6,330
26 - 27	9	24,720	8,205
28 - 29	7	18,215	8,207
30 - 31	5	18,500	7,000

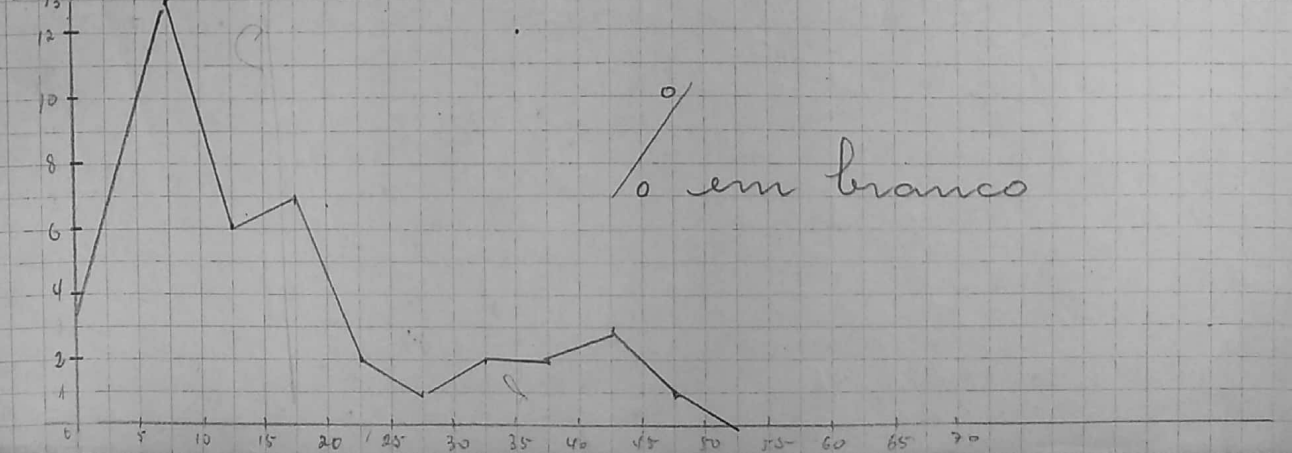
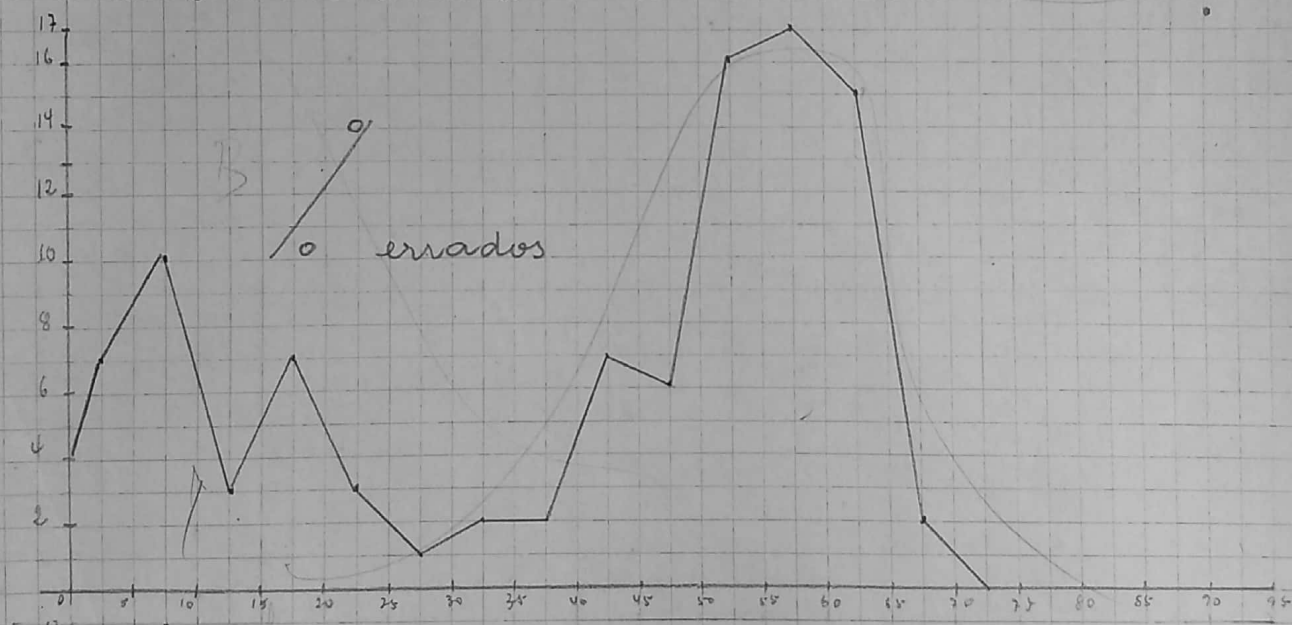
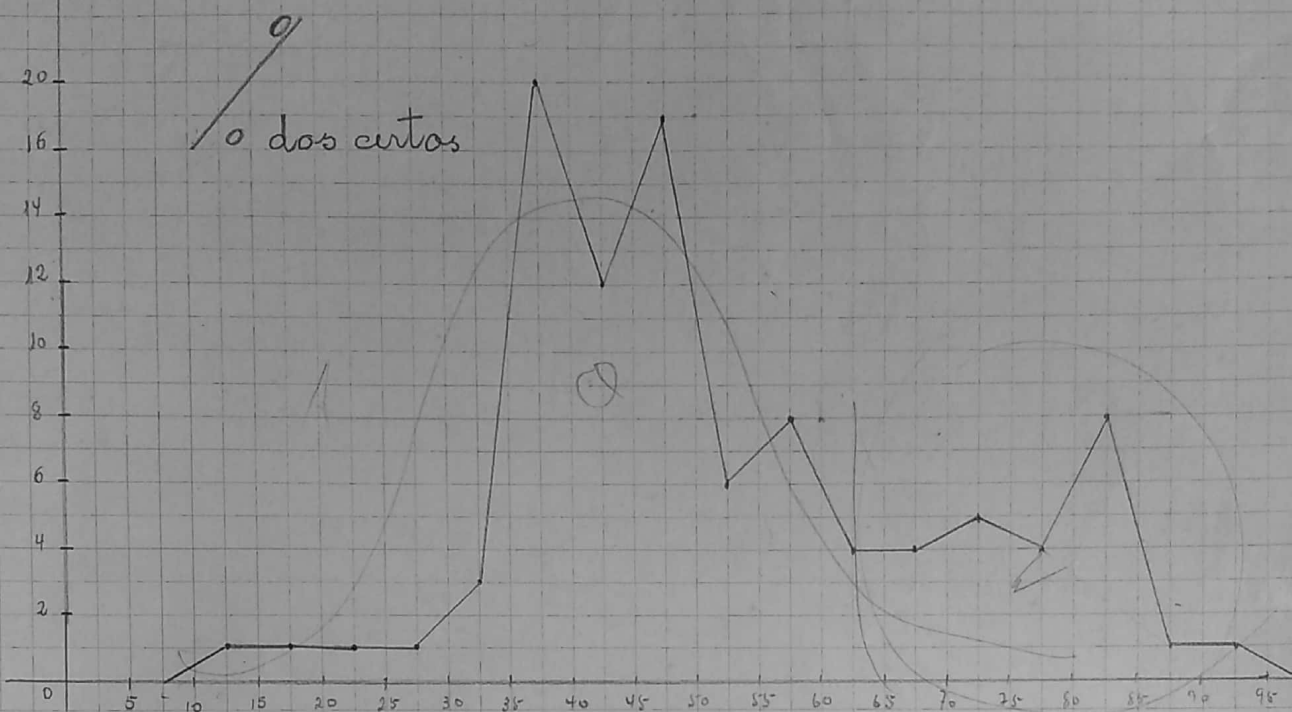
20

CALCULISTA

CURVA AJUSTADA - HISTOGRAMA DE FREQUÊNCIA
POLÍGONO DA DIFICULDADE DAS QUESTÕES - POLÍGONO DE FREQUÊN
CIA DAS NOTAS GDOBAL DE NIVEL MENTAL. - Sig. do '5"

Calculista do INEP e MTIC

Polígonos

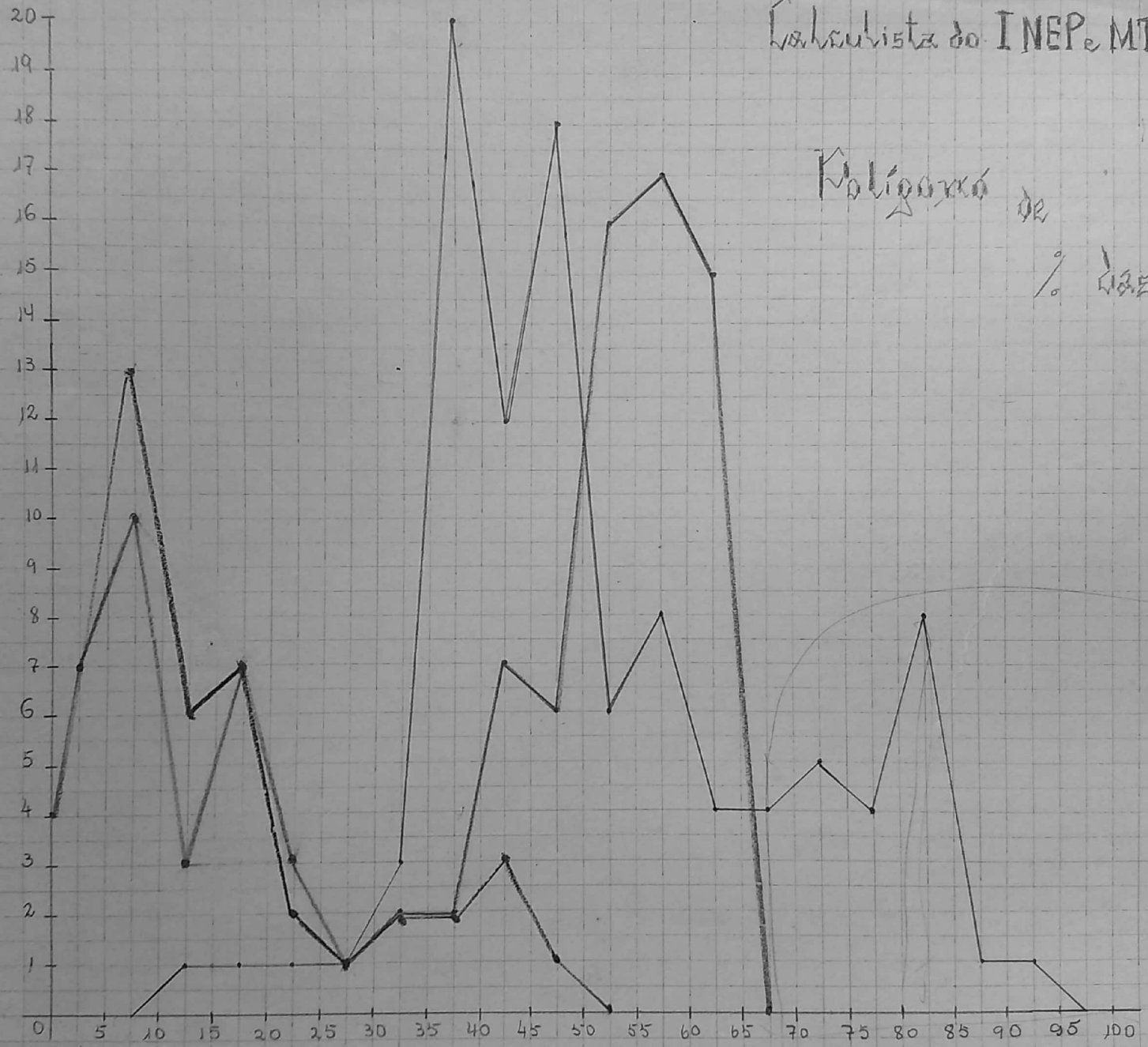


Calculista do INEP e MTIC

Nível Mental

Polygono de
% das Questões

Legenda
% certos —
% errados —
% em branco —



Grova de habilitação Calculista

idade X
estatística Y

VARIÁVEL X

	18	19	20	21	22	23	24	25	26	27	28	29	30	31	f	f ₀	f ₀ ²	f ₀ ³
0-4	5 ₅		4 ₁₅		1 ₅		1 ₅	1 ₁₀					1 ₃₅	2 ₈₀	12	5	-60	300
5-9	2 ₂₀	3 ₄₈	2 ₂₄		5 ₂₀		1 ₄		1 ₁₂		2 ₄₀	1 ₂₄			17	-4	-68	272
10-14	1 ₁₅	4 ₄₈	2 ₂₈		2 ₆	1 ₃	3 ₉							1 ₂₄	13	-3	-39	117
15-19	3 ₃₀	2 ₁₆	2 ₁₂	4 ₁₆	2 ₄			1 ₄		2 ₁₆	2 ₂₀				19	-2	-38	76
20-24	1 ₅	3 ₁₂	4 ₁₂	1 ₂					1 ₃						12	-1	-12	12
25-29															4			217
30-34		1 ₄		1 ₂		2	1 ₁								5	1	5	5
35-39		1 ₈	3 ₁₂			2		1 ₆							6	2	12	24
40-44						2	1 ₃	1 ₉							7	3	21	63
45-49	1 ₂₀					2	2 ₈		1 ₁₆		1 ₂₄				7	4	28	112
50-54	1 ₂₅	1 ₂₀	2 ₃₀	1 ₁₀	2 ₁₅				1 ₁₅						9	5	45	225
55-59	1 ₃₀	2 ₄₈	3 ₃₆	1 ₁₂	2 ₁₂					1 ₂₄			1 ₄₈		11	6	66	396
60				1 ₁₄							1 ₃₅				2	7	14	98
F	12	16	25	11	14	14	9	2	5	4	5	2	1	4	124	191	1700	
d	-5	-4	-3	-2	-1		1	2	3	4	5	6	7	8				
Fd	-60	-64	-75	-22	-14	-235	9	4	15	16	25	12	7	32	120	115		
Fd ²	300	256	225	44	14		9	8	45	64	125	72	49	256	1467			

VARIÁVEL X	VARIÁVEL Y	Coefficiente de correlação	Erro padrão de correlação
		$r = \frac{23 - 0,927 \times 0,210}{3,312 \times 1,8485}$	$\sigma_r = \frac{1 - 0,0008^2}{\sqrt{1,24}}$
$M = 23,5 - \frac{115}{124}$	$M = 27,5 - \frac{26}{124} \times 5$	$r = \frac{0,185184 - 0,194670}{61,222320} \times 5$	$\sigma_r = \frac{1 - 0,00000264}{11,134}$
$M = 22,573$	$M = 27,5 - 1,050$	$r = \frac{0,009196}{61,222320} \times 5$	$\sigma_r = \frac{0,97799936}{11,134}$
$\sigma = \pm \sqrt{\frac{1467 - 0,927^2}{124}}$	$M = 26,450$	$r = 0,00015 \times 5$	$\sigma_r = 0,090$
$\sigma = \pm \sqrt{1,830815 - 0,859329}$	$\sigma = \pm \sqrt{\frac{1716 - 0,210^2}{124}}$	$r = 0,00075$	\therefore
$\sigma = \pm \sqrt{10,971316}$	$\sigma = \pm \sqrt{13,709677 - 0,14100}$	$r = 0,0008$	
$\sigma = \pm 3,312$	$\sigma = \pm \sqrt{13,666577}$		
	$\sigma = \pm 5 \times 3,697$		
	$\sigma = \pm 18,485$		

VARIÁVEL Y



— Significância do "S" —

Calculista

$$M = 23,49$$

$$N = 131$$

$$\alpha = \frac{2f}{5} = 5,4$$

$$23,49 \times 5,4 = 126,846$$

$$46 + 126,846 = 172,846$$

$$\text{Sig. do } S = \frac{131}{2} \pm 3 \sqrt{\frac{131}{4}}$$

$$\text{Sig. do } S = 65,5 \pm 3 \sqrt{32,75}$$

$$\text{Sig. do } S = 65,5 \pm 3 \times 5,72$$

$$\text{Sig. do } S = 65,5 \pm 17,16$$

$$\text{Sig. do } S = 82,66 \text{ e } 48,34$$

Prova de habilitação

Calculista

$$N = 127$$

$$M = 23,485$$

$$M_i = 23,558$$

$$M_o = 23,704$$

$$\sigma = \pm 8,250$$

$$\sigma_M = 0,732$$

$$\sigma_{D.P.} = 0,518$$

$$S = -0,027$$

$$C.V. = 35,129$$

$$Q = 6,061$$

$$Q_1 = 17,546$$

$$Q_3 = 29,667$$

$$P_{15,87} = 15,40$$

$$P_{84,13} = 14,788$$

Candidatos que fizeram a prova de Nível mental e também a 2ª parte.

— polígono obtido
— curva normal ajustada.



Prova de habilitação

Calculista

$$N = 131$$

$$M = 23,490$$

$$M_i = 23,611$$

$$M_o = 23,853$$

$$\sigma = \pm 8,340$$

$$\sigma_M = 0,729$$

$$\sigma_{OP} = 0,515$$

$$S = -0,044$$

$$C.V. = 35,504$$

$$Q_1 = 17,546$$

$$Q_3 = 29,676$$

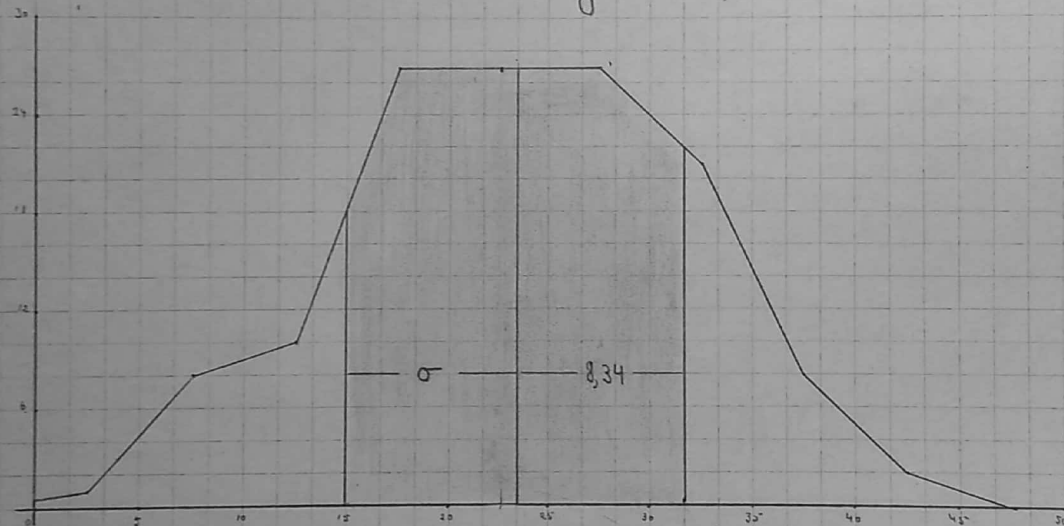
$$Q = 6,065$$

$$P_{15,87} = 15,331$$

$$P_{84,13} = 32,431$$

Nível mental

Polígono



Prova de habilitação Calculista

Nível mental

$$N = 131$$

$$M = 23,490$$

$$M_i = 23,611$$

$$\sigma = \pm 8,340$$

$$\sigma_M = \pm 0,729$$

$$\sigma_{DP} = \pm 0,515$$

$$M_0 = 23,853$$

$$S = -0,044$$

$$C.V. = 35,504$$

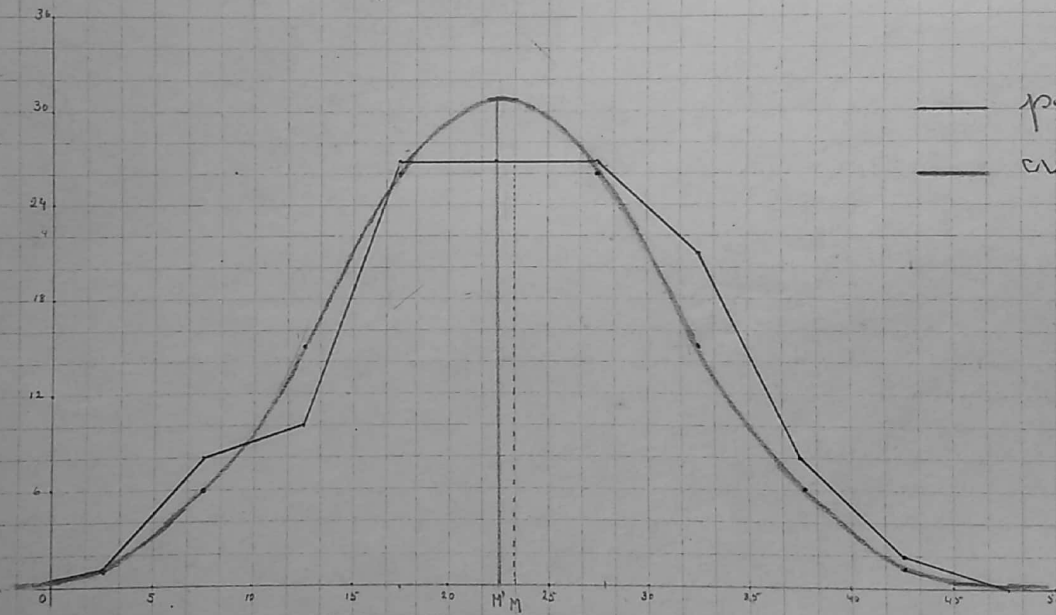
$$Q_1 = 17,546$$

$$Q_3 = 29,676$$

$$Q = 6,065$$

$$P_{15,97} = 15,331$$

$$P_{84,13} = 32,431$$



— polígono obtido
— curva normal ajustada

- $y_0 = 31,33$
- $y_1 = 26,17$
- $y_2 = 15,25$
- $y_3 = 6,20$
- $y_4 = 1,76$
- $y_5 = 0,35$

Prova de habilitação Calculista

$$N = 127$$

$$M = 23,485$$

$$M_i = 23,558$$

$$M_o = 23,704$$

$$\sigma = \pm 8,250$$

$$\sigma_M = 0,732$$

$$\sigma_{DP} = 0,518$$

$$C.V. = 35,129$$

$$S = 0,027$$

$$Q = 6,061$$

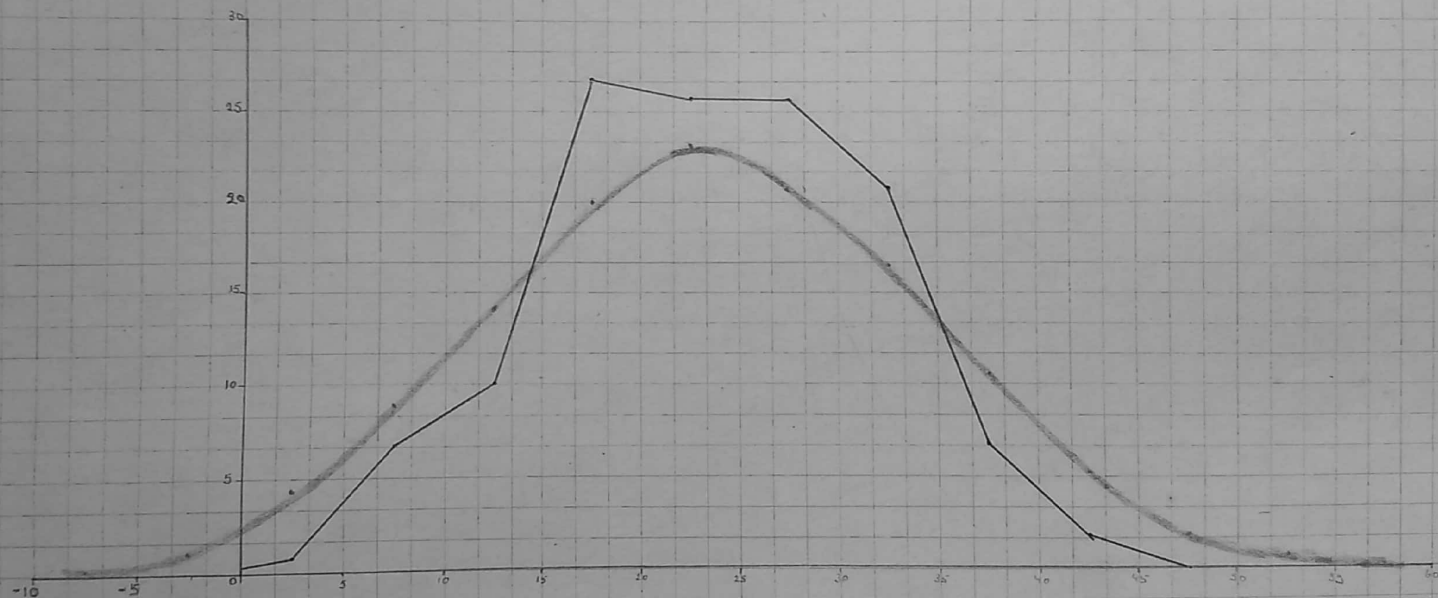
$$Q_1 = 17,546$$

$$Q_3 = 29,667$$

$$P_{15,87} = 15,40$$

$$P_{13,14} = 14,788$$

Curva ajustada (polinômio por per-equação)



Prova de habilitação

Calculista

Nível mental

Histograma

$$N = 131$$

$$M = 23,490$$

$$M_i = 23,611$$

$$M_o = 23,853$$

$$\sigma = \pm 8,340$$

$$\sigma_M = 0,729$$

$$\sigma_{D.P.} = 0,515$$

$$S = -0,044$$

$$CV = 35,504$$

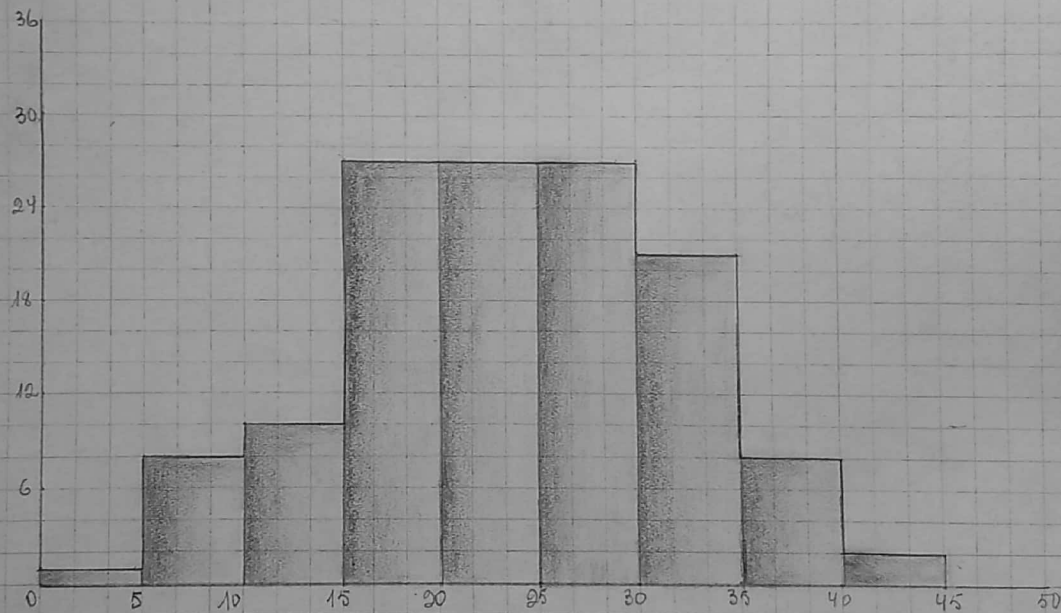
$$Q_1 = 17,546$$

$$Q_3 = 29,676$$

$$Q = 6,065$$

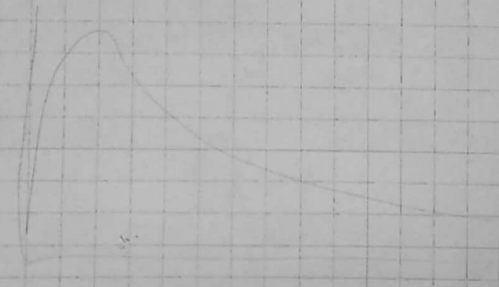
$$P_{15,97} = 15,331$$

$$P_{84,13} = 32,431$$



Prova de habilitação Calculista

Polígono da dificuldade das questões



X	Dif.
25 - 28	1
30 - 34	4
35 - 39	11
40 - 44	10
45 - 49	14
50 - 54	33
55 - 59	21
60 - 64	2
65 - 69	2
	98

